

**Applied Statistics for  
the Behavioral  
Sciences**

Chapter 10  
Two sample designs

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**Chapter Outline**

- Simple experiments
- Two-sample hypothesis testing
- Distinguishing between independent and correlated samples designs
- Calculation of t
  - Independent samples
  - Correlated samples
- Assumptions that accompany t
- Effect size
- Power
- Practical vs. statistical significance

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**Homework problems**

- Homework problems should be done both by hand and in SPSS until clearly understanding and able to run in SPSS w/o difficulty
- Problems on handout we will do in class both ways, work on your own ASAP

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### Simple experiment steps (p 201)

- Identify population
- **RANDOMLY** assign to groups
- Administer treatment (IV) [treatment A]
- Measure performance/behavior (DV) [task Q]
- Calculate means for groups (Descr. Stats.)
- Calculate effect size index  $\bar{X}_e$  &  $\bar{X}_c$
- Compare group means (Inferential statistics)
- Write a conclusion—in terms of original question

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### Experiments

- allow causal statements
- by randomly assigning to groups we've ruled out alternatives
- left with our intervention

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### Two-sample hypothesis testing (p 203-204)

- **two possibilities null and alternative hypothesis**  
 **$H_0$  : no effect, mean score for those receiving the treatment is equal to the mean for those not receiving [text – A vs. noA]**  
 **$H_0$  :  $\mu_{\text{treat}} - \mu_{\text{no treat}} = 0$  or  $H_0$  :  $\mu_{\text{treat}} = \mu_{\text{no treat}}$**   
 **$H_1$  :  $\mu_{\text{treat}} \neq \mu_{\text{no treat}}$  (2 tailed) or either**  
 **$H_1$  :  $\mu_{\text{treat}} > \mu_{\text{no treat}}$  or  $\mu_{\text{treat}} < \mu_{\text{no treat}}$  (1 tailed)**

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### Two-sample hypothesis testing

- *assume equality hypothesis correct If null true: samples vary only by extent of sampling error*
- *select alpha level (almost always will be .05)*
- *choose an inferential statistic (for now just need to decide which t, independent or correlated samples)*
- *calculate test statistic from sample data*

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### Two-sample hypothesis testing

- *compare the test statistic with the critical value from the statistic's sampling distribution*
  - if the t value obtained from the data exceeds t critical (or probability < alpha) we can reject the null*
  - if probability is greater than alpha (or statistic doesn't exceed critical value) retain the null.*
- *formulate a conclusion/interpretation – again in the terms of the original question*

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### Independent vs. correlated t tests

- *basic idea is taking a difference observed, divide by standard error of the difference giving a t statistic*
- *Three types of correlated designs:*
  - Natural pairs*
  - Matched pairs*
  - Repeated measures*
- *Independent samples*
  - no way to pair observations*

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## Calculation of t

- Independent samples design

$$\square df = N_1 + N_2 - 2$$

$$t = \frac{\bar{X}_1 - \bar{X}_2}{S_{\bar{X}_1 - \bar{X}_2}}$$

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## Standard error of difference

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{s_{\bar{X}_1}^2 + s_{\bar{X}_2}^2}$$

- If  $N_1 = N_2$ 

$$= \sqrt{\left(\frac{\hat{s}_1}{\sqrt{N_1}}\right)^2 + \left(\frac{\hat{s}_2}{\sqrt{N_2}}\right)^2} = \sqrt{\frac{\sum X_1^2 - \frac{(\sum X_1)^2}{N_1} + \sum X_2^2 - \frac{(\sum X_2)^2}{N_2}}{N_1(N_2 - 1)}}$$

- If  $N_1 \neq N_2$ 

$$s_{\bar{X}_1 - \bar{X}_2} = \sqrt{\frac{\sum X_1^2 - \frac{(\sum X_1)^2}{N_1} + \sum X_2^2 - \frac{(\sum X_2)^2}{N_2}}{N_1 + N_2 - 2} \left(\frac{1}{N_1} + \frac{1}{N_2}\right)}$$

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## Independent samples T

- Lazarus data
- Do by hand
- Later in SPSS, answers should match

	Detached	Involved
	23	31
	21	27
	19	24
	15	23
	14	21
	12	14
	10	

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## Effect size

- Cohen's d statistic, same as one-sample case
- Interpretation is identical
- Tells us how much of an effect the independent variable had

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## Effect size index

- Independent samples  $d = \frac{\bar{X}_1 - \bar{X}_2}{\hat{s}}$

- if  $N_1 = N_2$ ,  $\hat{s} = \sqrt{N_1}(s_{\bar{x}_1 - \bar{x}_2})$

- If  $N_1 \neq N_2$ ,  $\hat{s} = \sqrt{\frac{\hat{s}_1^2(df_1) + \hat{s}_2^2(df_2)}{df_1 + df_2}}$

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## Correlated samples t-test

- $df = N - 1$  where  $N$  = number of pairs of scores

$$t = \frac{\bar{X} - \bar{Y}}{s_{\bar{D}}}$$

- Formula illustrates effect r has

$$s_{\bar{D}} = \sqrt{s_{\bar{X}}^2 + s_{\bar{Y}}^2 - 2r_{XY}(s_{\bar{X}})(s_{\bar{Y}})}$$

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## Direct difference method

- does not require calculating r first

$$t = \frac{\bar{X} - \bar{Y}}{s_{\bar{D}}} = \frac{\bar{X} - \bar{Y}}{\hat{s}_D / \sqrt{N}} \quad \hat{s}_D = \sqrt{\frac{\sum D^2 - (\sum D)^2}{N-1}}$$

- $D = X - Y$
- $N =$  number of pairs of scores

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## Correlated Samples t – example

- Two cats from each litter randomly assigned to each group
- Amount of alcohol laced milk they drank was measured

Littermates	No Experimental Neurosis	Experimental Neurosis
1	63	88
2	59	90
3	52	74
4	51	78
5	46	78
6	44	61
7	38	54

- Perform a t-test, an effect size index and calculate 99% confidence interval.

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## Effect size index

- For correlated samples, same general formula:

$$d = \frac{\bar{X} - \bar{Y}}{\hat{s}}$$

- Difference is in  $\hat{s} = \sqrt{N}(s_{\bar{D}})$

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## Assumptions of t

- dependent variable normally distributed
- dv variance = across groups
- samples randomly selected
- t test is robust to violations of assumptions

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## Final issues

- Power
  - only way we are able to control power is via sample size
  - comparing groups want to be certain we're using a relatively sensitive measure that will reveal group differences of a reasonable magnitude
- Practical vs. statistical significance
  - Finding statistical significance tells us nothing about the practical or clinical significance of a research finding – effect size plays a role here

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