Applied Statistics for the **Behavioral Sciences**

Probability and Theoretical Distributions including the Normal Distribution Chapter 7

Outline

- Probability
- Distributions
 - rectangular
 - binomial
 - normal
- Using the normal curve to find probabilities
- Let's watch a movie...For All Practical Purposes – Place Your Bets – on your own

Probability: Measuring Uncertainty

- We're all familiar on some level with probability.
- Examples are all over in language: "chances are," "maybe," and "probably" all suggest an intuitive understanding of probability.
- □ Statements: 2 parts
 - an event the probability of that event
- Certain events
 - Definitely will or will not happen p(event) = either 0 or 1

Probability (cont.)

Uncertain events have p between 0 - 1

- $\ensuremath{\,\square}$ expresses the degree of uncertainty
 - A. P(heads with a fair coin)=.50
 - B. P(drawing ace of hearts from full deck)=.019
 - C. P(rolling a three with a fair die)=.167
- Each of these is a success, (k), other outcome is a failure (j), P(success)=k/(k+j)
- Ways of expressing probabilities
 - P(A) = .50 or ½ or 50% or 50-50 or 1 to 1
 - P(B) = .019 or 1/52 or 1.9% or 51 to 1 against

Calculating probabilities

- Each possible outcome is an elementary event
- Count the number of elementary events in each outcome class
- □ If each elementary event equally likely, probability of outcome class A can be easily computed
- p(A)=# of elem. events that are A/ Tot # of elementary events (same as saying k/(k+j)
- This holds only if the elementary event is a truly random event.
- Over many trials the proportion of "A" outcomes will approach p(A), with enough trials the empirical distribution will look more and more like the theoretical distribution

Different orders

- **5** people milling around
- What is the probability that they will line up in alphabetical order?
- N of different ways can they line up in alphabetical order?
- 2, this is the numerator
- What goes in the denominator?
 - Total number of different ways 5 people can line up (5! – what does this mean?)
- **\square** P(line up alphabetically) = .017

Distributions

- Theoretical distributions always have a total area of 1.0
- statements about area are equivalent to statements about probability

Rectangular

- **p**g. 131 text
- playing cards
- disregarding suit, 13 different cards, p(any particular card)=.077
- probabilities can be additive, p(7, 8, or 9)=.231 (.077*3) or 12/52=.231
- **•** if we actually drew 52 times from a deck would deviate from theoretical rectangular dist.
- Empirical and theoretical distributions

Binomial

- Essential element- event(s) with two possible outcomes Pg. 132
- □ flip three coins (for independent events, we can simply multiply the probabilities of the events) .5x.5x.5 = .125eight possible outcomes
- hhh, hht, hth, thh, htt, tht, tth, ttt
- each has a P of .125 (1/8)
- **b** for heads, p(0)=.125, p(1)=.375, p(2)=.375, p(3)=.125 • over enough real trials we will end up with an empirical
- distribution very close to the theoretical not exactly the same, but close

Standard Normal Curve

- \blacksquare μ = 0.0 and σ = 1.0
- X-axis on a standard normal curve is often relabeled and called z scores

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page 400 Table of areas under normal curve-mark it somehow for quick access













Area under Normal Curve

we can compute additional areas
area between a Z-score of 0.0 and 1.0
take 1/2 the area between -1.0 and 1.0
Why?

Area under Normal Curve

- the distribution is symmetrical between those two points
- □ answer in this case is .34 or 34%
- same for the area between 0.0 and -1.0

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Areas under Normal Curve

area below a Z-score of 1.0?

- computed by adding .34 and .50 to get .84
- area above a Z-score of 1.0?
- subtract the area just obtained from the total area under the distribution (1.00)

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1.00 - .84 or .16 or 16%

Areas under Normal Curve

area between -2.0 and -1.0?

- □ first, the area between 0.0 and -2.0 is 1/2 of .95 or .475
- the .475 includes too much area, the area between 0.0 and -1.0 (.34) must be subtracted from this
- □ so, .475 .34 or .135





Using normal curve – example

Mean = 10, SD = 2

- What proportion of scores is between 7.5 & 12.5?
- What proportion of scores is between 7.5 & 10.5?
- What score separates the lower 40% from the upper 60%?
- If there were 250 members of population, how many would be expected to score 11 or more?
- What proportion would be expected to score 9 or more?
- What score separates the top 10% of scores from the rest?
- Does this problem deal with a theoretical or empirical distribution?
- Always sketch a picture!
- There will be a problem very similar to this on exam 3!! 19